

Modelling Contextual Effects in Oral Health Disparities

Hands-On workshop: Multilevel Models in R

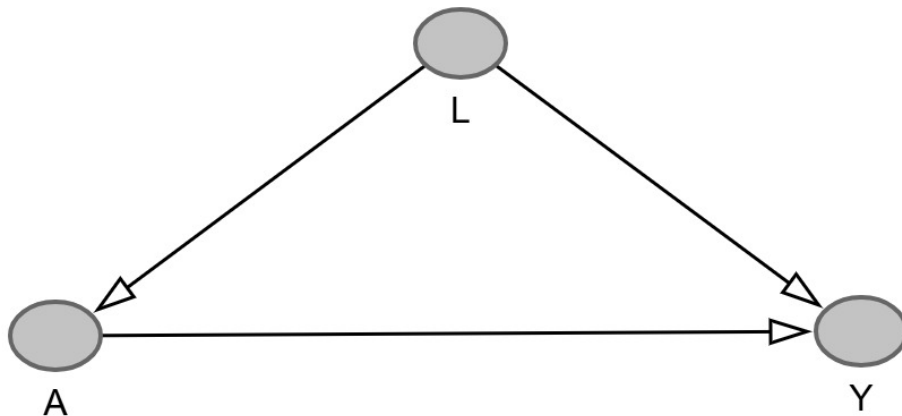
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Conflict of interest

No disclosure

Directed Acyclic Graph

Question: Is high dental pain prevalence among school kids simply due to high sugar consumption of individual kids?



Exposure (A): Dichotomized sugar consumption

Outcome (Y): Dental pain (Yes/No)

Level 1 confounders (L1): Sex, Age, family income

Level 2 confounder (L2): School type (Private/Public)

Cluster: School

Contextual effects estimation: Hands-on in R

1. Core Concepts

- General Contextual Effects (GCE) & Specific Contextual Effects (SCE)

2. Key Metrics

- Variance Partition Coefficient (VPC)/Intraclass Correlation Coefficient (ICC)
- Median Odds Ratio (MOR)

3. Multilevel Modelling Strategy

4. Hands-on Demonstration

- Contextual effects estimation using simulated data in R

Contextual Effects

Aspect	General Contextual Effects (GCE)	Specific Contextual Effects (SCE)
Core meaning	Overall influence of the place/context itself (often unobserved)	Place adds effect via measured factors (e.g. school type)
Oral health example	Different dental pain prevalence in different schools even after individual factors adjustment	Higher dental pain prevalence in public schools persists after full adjustment — due to poor fluoride access, fewer dentists, food environment etc.
Estimation	Variance Partition Coefficient (VPC) / Intraclass Correlation Coefficient (ICC)/ Median Odds Ratio (MOR) for binary outcome	Fixed OR for higher level variable

Diez Roux (2002); Merlo, et al. (2018)

Variance Partition Coefficient (VPC)

- The proportion of the total variance that is attributable to a particular level
- VPC attributable to the higher level: often used interchangeably as Intraclass Correlation Coefficient (ICC)

$$VPC = \frac{\sigma_u^2}{\sigma_u^2 + \sigma_e^2}$$

- $\sigma_e^2 = \frac{\pi^2}{3} = 3.29$ when outcome is binary
- VPC varies with covariate values if random slopes present

Snijders and Bosker RJ (2012)

Median Odds Ratio (MOR)

- $MOR = e^{\phi^{-1}(0.75)\sqrt{2\sigma_u^2}}$

σ_u^2 = estimated variance of the random intercepts (between-group variance) from the multilevel logistic model

$\phi^{-1}(0.75) \approx 0.6745$ (the 75th percentile of the standard normal distribution)

- How much the odds of the outcome would (typically) increase (in the median case) if a person moved from a lower-risk cluster to a higher-risk cluster — everything else being equal.
- It directly reflects the impact of the clustering/context on the individual outcome.

Multilevel Modelling Strategy

Model	Predictors added	Purpose
M0	None (empty random intercept)	Baseline clustering (VPC/ICC)—how much variation is between clusters
M1	Main exposure only	Crude association between exposure and outcome, accounting for clustering
M2	Main exposure + compositional confounders	Compositional effects—how much of the exposure and outcome difference is due to who lives/attends there
M3	Main exposure + compositional confounders+ contextual confounders	Best estimate of true contextual/place-based effect

Multilevel Modelling

```
##Model 0: Two-level variance-components binomial model
M0 <- glmer(dental_pain ~ 1 + (1|school_id), data = Pain,
            family = binomial(link="logit"))

# Model 1: Two-level Random Intercept binomial model with exposure only
M1 <- update(M0, . ~ . + high_sugar)

# Model 2: Two-level Random Intercept binomial model adjusted
##by level 1 confounders
M2 <- update(M1, . ~ . + age_c + sex + family_income)

# Model 3: Two-level Random Intercept binomial model adjusted by
##all confounders
M3 <- update(M2, . ~ . + school_type)
```

Results: M0

```
## Results of M0
summary(M0)

## probability of
## having pain
plogis(fixef(M0))
#Observed prevalence
mean(Pain$dental_pain)
```

```
Generalized linear mixed model fit by maximum likelihood (Laplace Approximation) ['glmerMod']
Family: binomial ( logit )
Formula: dental_pain ~ 1 + (1 | school_id)
Data: Pain
```

AIC	BIC	logLik	-2*log(L)	df.resid
6301.1	6314.2	-3148.6	6297.1	4998

```
Scaled residuals:
  Min      1Q  Median      3Q      Max
-1.8974 -0.7440 -0.5083  0.9823  2.5854
```

```
Random effects:
 Groups   Name      Variance Std.Dev.
school_id (Intercept) 0.6977  0.8353
Number of obs: 5000, groups: school_id, 300
```

```
Fixed effects:
              Estimate Std. Error z value Pr(>|z|)
(Intercept) -0.59988    0.05836  -10.28  <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
> plogis(fixef(M0))
(Intercept)
  0.3543713
> #Observed prevalence
> mean(Pain$dental_pain)
[1] 0.374
```

Restricted, Sensitive (Normal)

Results: M0

```
# manual VPC in a tidy way  
var_u <- VarCorr(M0)$school_id[1,1]  
vpc <- var_u / (var_u + pi^2 / 3)  
var_u  
vpc
```

```
> var_u  
[1] 0.6977395  
> vpc  
[1] 0.174977
```

```
# VPC with performance  
icc(M0)
```

```
# Intraclass Correlation Coefficient
```

```
Adjusted ICC: 0.175  
Unadjusted ICC: 0.175
```

VPC/ICC

```
models <- list(M0 = M0, M1 = M1, M2 = M2, M3 = M3)
```

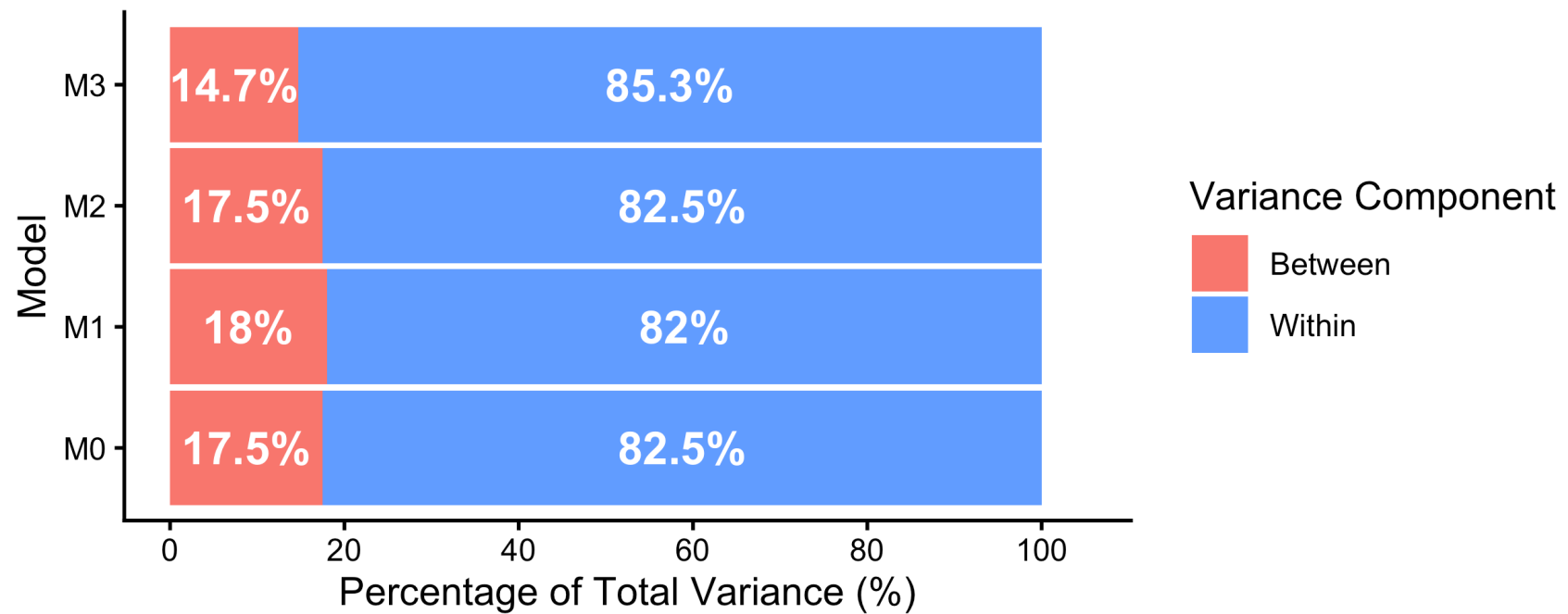
```
vpc_table <- map(names(models), ~ tibble(  
  Model = .x,  
  VPC_percent = round(icc(models[[.x]])$ICC_adjusted[1] * 100, 1),  
  School_Var = VarCorr(models[[.x]])$school_id[1, 1]  
)) %>% list_rbind()
```

```
vpc_table %>% print()
```

	Model	VPC_percent	School_Var
	<chr>	<dbl>	<dbl>
1	M0	17.5	0.698
2	M1	18	0.721
3	M2	17.5	0.700
4	M3	14.7	0.565

Restricted, Sensitive (Normal)

VPC/ICC



Final model: M3

```
tidy(M3, conf.int = TRUE, exponentiate = TRUE) %>%
  filter(effect == "fixed") %>%
  dplyr::select(term, estimate, std.error, statistic, p.value, conf.low, conf.high) %>%
  mutate(across(where(is.numeric), ~ round(., 3)))
```

A tibble: 6 × 7

term	estimate	std.error	statistic	p.value	conf.low	conf.high
<chr>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>	<dbl>
1 (Intercept)	0.144	0.02	-13.8	0	0.109	0.189
2 high_sugarhigh	2.28	0.156	12.0	0	1.99	2.61
3 age_c	1.05	0.035	1.58	0.114	0.987	1.12
4 sexfemale	1.30	0.085	4.10	0	1.15	1.48
5 family_incomelow	1.16	0.082	2.08	0.037	1.01	1.33
6 school_typepublic	2.78	0.405	7.00	0	2.09	3.70

Specific Contextual Effect: OR=2.78 (2.09, 3.70)

Final model: M3

General Contextual Effect

```
##General contextual effect  
# MOR: for use with the multilevel logistic regression model  
# var_u denote the estimate variance of the random effects.  
var_u=VarCorr(M3)$school_id[1,1]  
MOR <- exp(((2*var_u)^0.5)*qnorm(0.75))  
MOR
```

> MOR

[1] 2.048593

Single level model

```
M_SL <- glm(dental_pain ~ high_sugar + age_c + sex + family_income + school_type,
           data = Pain, family = binomial(link="logit"))
tidy(M_SL, conf.int = TRUE, exponentiate = TRUE) %>%
  dplyr::select(term, estimate, std.error) %>%
  mutate(across(where(is.numeric), ~ round(., 3)))
```

A tibble: 6 × 7

term <chr>	estimate <dbl>	std.error <dbl>
1 (Intercept)	0.176	0.091
2 high_sugarhigh	2.11	0.063
3 age_c	1.05	0.031
4 sexfemale	1.31	0.06
5 family_incomelow	1.13	0.066
6 school_typepublic	2.49	0.088

A tibble: 6 × 7

term <chr>	estimate <dbl>	std.error <dbl>
1 (Intercept)	0.144	0.02
2 high_sugarhigh	2.28	0.156
3 age_c	1.05	0.035
4 sexfemale	1.30	0.085
5 family_incomelow	1.16	0.082
6 school_typepublic	2.78	0.405



Restricted, Sensitive (Normal)



Summary

- Contextual effects should be considered when investigating associations between exposures and oral health outcomes — ignoring them risks incomplete or biased explanations of disparities.
- Both General Contextual Effects (GCE: ICC/MOR/residual clustering) and Specific Contextual Effects (SCE: fixed ORs for measured high level factors) provide complementary insights.
- Multilevel regression is the recommended methodology to properly quantify, distinguish, and interpret these effects in oral health disparities research.

References

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- Snijders TAB, Bosker RJ (2012) *Multilevel analysis: an introduction to basic and advanced multilevel modeling*. Sage, Los Angeles

Thank you!

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